

3.18 The free energy as an example for a thermodynamic potential

The **free energy** is the corresponding thermodynamic potential for the thermal contact of section 3.15.

Therefore the corresponding coordinates are V, N , and T .

It is well known that

$$F(V, N, T) = U(V, N, T) - S(V, N, T)T \quad (3.32)$$

and

$$dF = \mu dN - pdV - SdT \quad (3.33)$$

Mathematical interpretation: total differential, partial derivative

$\left. \frac{\partial F}{\partial N} \right _{V,T} = \mu$	$\left. \frac{\partial F}{\partial V} \right _{N,T} = -p$	$\left. \frac{\partial F}{\partial T} \right _{V,N} = -S$
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Physical interpretation: gradient, forces

μ : "force" changing the particle number	$-p$: "force" changing the volume	$-S$: "force" changing the temperature
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here: V, N, T : generalized coordinates

$-p, \mu, -S$: generalized forces

For "normal" physical quantities:

Coordinates: extensive parameters

Forces: intensive parameters

Forces and coordinates can be exchanged. There exists no fundamental difference between these parameters since they are equivalent and just depend on the choice of the thermodynamic contact.