26 Statistical Mechanics

2.2 The microcanonical, canonical, and the grandcanonical ensemble

The macro state has to be considered by its restrictions.

micro restrictions	macro restrictions	
Each system of the ensemble, even each micro state fulfills the restriction	Only on average the ensemble fulfills the restriction	
e.g. $U_i = U$	e.g. $\sum_{i} p_i U_i = U$	

For large systems $(N \gg 1)$ micro- and macro restrictions do not differ in their physical properties.

Kind of	micro restriction	macro restrictions	macro restrictions
ensemble	Average only of systems with identical values of:	variable values for averaging	averages
micro canon- ical ensemble	V, N, U		
canonical ensemble	V, N	U_i	$U = \sum_{i} p_i U_i$
grand canonical ensemble	V	$egin{array}{c} U_i \ N_i \end{array}$	$U = \sum_{i} p_{i} U_{i}$ $N = \sum_{i} p_{i} N_{i}$

This ensembles correspond to different thermodynamic contacts.

Which ensemble we use for the calculation is just a question of convenience.